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#### **Physics Concerto Seminar Series**

 $\bar{\text{S}}\text{upported}$  by the Weinberg Institute for Theoretical Physics, Department of Physics, University of Texas

### Beyond the Big Bang: Delving into Inflationary Cosmology

Gabriele Montefalcone

P.h.D. Candidate, Weinberg Institute for Theoretical Physics, University of Texas at Austin



BRIDGING PHYSICS SPECIALTIES THROUGH PEER TO PEER SEMINARS

# History of the universe



A.J.S. Hamilton, Modern Cosmology https://jila.colorado.edu/~ajsh/courses/as tr2010\_22/index.html

# History of the universe



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#### Outline

- properties of our universe and big bang cosmology
- the shortcomings of the big bang model
- cosmic inflation
- challenges and shortcomings of the inflationary picture

#### The Cosmological Principle



$$G_{\mu\nu} = 8\pi G T_{\mu\nu}$$

- describes the geometry and curvature of spacetime
- it is a function of the metric  $g_{\mu
  u}$

encodes how much "stuff" (matter, energy, momentum, pressure, etc.) is present at each spacetime point

$$ds^2 = g_{\mu\nu} dx^\mu dx^\nu$$

• Cosmological principle  $\rightarrow$  FRW metric:

$$ds^2 = -dt^2 + \underbrace{a(t)^2}_{\text{the scale factor}} \left( \frac{1}{1 - kr^2} dr^2 + r^2 d\Omega^2 \right)$$

• Only three possibilities: k={1,0,-1}



J. Schombert, Cosmology https://pages.uoregon.edu/jschombe/cosmo/l ectures/lec15.html

• Cosmological principle + perfect fluid  $\rightarrow$  Diagonal  $T_{\mu\nu}$ 

$$T^{00} = -\rho, \qquad T^{jj} = p.$$

• Friedmann Equations:

$$\frac{\ddot{a}}{a} = -\frac{4\pi G}{3}\rho(1+3\omega)$$

• Fluid Equation:

$$rac{\dot{
ho}}{
ho} = -3H(1+w) \ \omega \equiv p/
ho$$

$$\left(\frac{\dot{a}}{a}\right)^2 = \frac{8\pi G}{3}\rho - \frac{k}{a^2}$$
$$\frac{\dot{a}}{a} \equiv H \quad \text{(The Hubble parameter)}$$



• Matter:  $p_m \ll \rho_m \rightarrow \omega_m \simeq 0$ :  $a(t) \sim t^{2/3}$ 

• Radiation: 
$$p_r = \frac{1}{3} \rho_r \rightarrow \omega_r = \frac{1}{3}: \quad a(t) \sim t^{1/2}$$

• Vacuum: 
$$p_v = -\rho_v 
ightarrow \omega_v = -1:$$
  $a(t) \sim e^{Ht}$ 

Note, a convenient notation:  $\Omega_j=
ho_j/
ho_c$  .

(the jth energy density parameter)

$$\rho_c \equiv \frac{3H^2}{8\pi G}$$

(the critical energy density)

• Friedmann Equations:

$$\frac{\ddot{a}}{a} = \frac{8\pi G}{3}\rho(1-\epsilon)$$

$$\epsilon \equiv rac{3}{2}(1+\omega)$$
 (The Hubble slow-roll parameter)

The universe accelerates if  $\varepsilon < 1!$ 

• The Friedmann equation can be rewritten as:

$$1 - \sum_{j} \Omega_{j} = \Omega_{k}$$
$$\Omega_{k} \equiv -\frac{k}{a^{2}H^{2}}$$
$$\Omega \equiv \sum_{j} \Omega_{j}$$

Note, a convenient notation:  $\Omega_j=
ho_j/
ho_c$ 

(the jth energy density parameter)

$$\rho_c \equiv \frac{3H^2}{8\pi G}$$

(the critical energy density)

A.J.S. Hamilton, Modern Cosmology <u>https://jila.colorado.edu/~ajsh/courses/as</u> <u>tr2010 22/index.html</u>



#### The shortcomings of Big Bang Cosmology The flatness problem

- We live in a FLAT universe
  - $\circ$  Present observations suggest that  $| {old \Omega}_{
    ho} ext{--}1 | \lesssim 10^{-3}$
- Necessity of an extreme fine tuning of the initial value of  $\Omega$ .  $|\Omega - 1| \propto t$  (radiation domination)  $|\Omega - 1| \propto t^{\frac{2}{3}}$  (matter domination)
  - $\circ~$  this implies  $|\Omega^{-1}| \lesssim 10^{-16}$  at nucleosynthesis epoch, and  $|\Omega^{-1}| \lesssim 10^{-64}$  at Planck epoch.



#### The shortcomings of Big Bang Cosmology The Horizon problem

- The universe at the time of decoupling was in *thermal* equilibrium, yet there had not been enough time for distant regions to be in casual contact.
  - $\circ~$  CMB consist of  ${\sim}10^5$  causally disconnected regions.



D. Baumann, TASI Lectures on Inflation, arXiv0907.5424

#### The shortcomings of Big Bang Cosmology The Monopole problem

- All Grand Unified Theories predict the existence of magnetic monopoles, extremely heavy particles with net magnetic charge.
- If these particles exist in the early universe, they could be the dominant materials in the universe, yet we do not observe them.

### **Cosmic Inflation**

• A period of accelerated expansion in the early universe

- Explains the observed flatness, homogeneity, and the lack of relic monopoles
- Provides with a mechanism for generating the inhomogeneities observed in the Cosmic Microwave Background



<u>https://breakthrou ghprize.org/Laurea tes/1/L2</u>

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		Dec 7, 1979
Ī	SPECTACULAR REALIZATION ;	
	This kind of supercooling can explain	why
	the universe today is so incredibly flat	- and
	therefore why resolve the fine-tuning par	adox
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<u>https://www.symmetrymagazine.org/article/december-2004january-2005/inflation?language</u> \_\_content\_entity=und

#### **Cosmic Inflation**

• Single scalar field minimally coupled to gravity

$$S_{\phi} = \int d^4x \sqrt{-g} \left[ \frac{1}{2} \partial_{\mu} \phi \partial^{\mu} \phi - V(\phi) \right]$$

• Slowly-rolling homogeneous field that dominates the energy density of the universe induces an *exponential* expansion

$$V(\phi) \gg \dot{\phi}^2$$

$$T_{\mu\nu} = \frac{2}{\sqrt{-g}} \frac{\delta S_{\phi}}{\delta g^{\mu\nu}} \begin{cases} \rho_{\phi} = -T_{00} = \frac{1}{2} \dot{\phi}^2 + V(\phi) + \frac{\nabla^2 \phi}{2} \\ p_{\phi} = \frac{1}{3} T_j^j = \frac{1}{2} \dot{\phi}^2 - V(\phi) - \frac{\nabla^2 \phi}{6} \end{cases} \longrightarrow \epsilon_{\phi} \equiv \frac{\frac{3}{2} \dot{\phi}^2}{\frac{\dot{\phi}^2}{2} + V(\phi)} \\ \ddot{a} > 0 : \epsilon_{\phi} < 1 \\ \sim 0 \end{cases}$$

#### **Cosmic Inflation**

$$H^2 \simeq \frac{8\pi G}{3} V(\phi) \longrightarrow a(t) \sim e^{Ht}$$

 Accelerated expansion will only be sustained if the second time derivative of the field is small enough

 $|\ddot{\phi}| \ll |3H\dot{\phi}|, |V_{,\phi}| \, . \label{eq:phi_eq}$ 

$$\eta \equiv -\frac{\ddot{\phi}}{H\dot{\phi}} = \varepsilon - \frac{1}{2\varepsilon}\frac{d\varepsilon}{dN} < 1$$

(The number of e-foldings)



D. Baumann, TASI Lectures on Inflation, arXiv0907.5424

$$N \equiv \ln(a_f/a_i) = \int_{t_i}^{t_f} H dt$$

#### The successes of Inflation The flatness problem

- During inflation:  $|\Omega-1| \propto e^{-2Ht^2}$
- To solve the flatness problem we need at the end of inflation:

$$|\Omega_f - 1| \lesssim 10^{-60}$$

$$\frac{|\Omega_f - 1|}{|\Omega_i - 1|} \simeq \left(\frac{a_i}{a_f}\right)^2 = e^{-2N}$$

 Roughly 70 e-folds of inflation solve this issue! J. Schombert, Cosmology https://pages.uoregon.edu/jschombe/cosmo ectures/lec15.html



# The successes of Inflation

- The superluminal accelerated expansion stretches a small causally connected patch, to large cosmological scales works.
- Once again, roughly 70 e-folds of inflation are sufficient to solve this issue.



# The successes of Inflation The Monopole problem

• Simply arrange the parameters such that inflation takes place after (or during) monopole production, so the monopole density is *diluted* to a completely negligible level.

#### **The successes of Inflation** CMB anisotropies

- Provides a mechanism for generating the inhomogeneities observed in the Cosmic Microwave Background
- Quantum fluctuations are driven to cosmological scales via the expansion

$$\frac{\delta T}{T} \sim \frac{\delta \rho}{\rho} \propto \langle \delta \phi^2 \rangle^{1/2}$$

Planck Collaboration <u>https://www.esa.int/ESA\_Multimedia/Images/</u> 2013/03/Planck\_CMB



### Summary

- Inflation is a cosmological theory proposing a *rapid and exponential* expansion of the universe in its early moments, resolving several long-standing problems in cosmology (homogeneity, flatness, unwanted relics, origin of cosmic structures)
- Inflation is simple: a single scalar field, minimally coupled to gravity, and slowly-rolling down a nearly flat potential, does the job.

#### Maybe not so simple? A list of long-standing concerns

- Multiverse Hypothesis, i.e. eternal inflation
- Measure problem: are we the most likely patch of the universe?
- Initial conditions problem: are these generic or need to be fine-tuned?
- Tuning of the Inflationary model: for some, a high-degree of fine-tuning is needed to fit observations
- **Quantum gravity concerns:** Inflation's early moments involve extremely high energies, where the effects of quantum gravity may not be negligible
- How do we actually **reheat** the universe?